

Happy Wednesday!

- Please place cell phones in holder.

-Remember test moved to Monday!

Finding the Inverse

Of An Exponential Function

1. Switch x and y
2. Solve for the base
3. Convert to a log
4. Solve for y

Example 1 $y = 2^{x-3} + 4$

$$x = 2^{y-3} + 4$$

$$x - 4 = 2^{y-3}$$

$$\log_2(x-4) = y-3$$

Example 2 $y = 3 \cdot 2^{2x-1}$

$$\log_2(x-4) + 3 = y^{-1}$$

$$\frac{1}{2}x = 3 \cdot 2^{2y-1}$$

$$\frac{x}{3} = 2^{2y-1}$$

$$\log_2\left(\frac{x}{3}\right) = 2y-1$$

$$\log_2\left(\frac{x}{3}\right) + 1 = 2y$$

$$\frac{1}{2} \log_2\left(\frac{x}{3}\right) + \frac{1}{2} = y^{-1}$$

$$\frac{\log_2\left(\frac{x}{3}\right) + 1}{2} = y^{-1}$$

Of A Logarithmic Function

1. Switch x and y
2. Solve for the log
3. Convert to a exponential
4. Solve for y

Example 3 $y = \log_3(x-2)$

$$x = \log_3(y-2)$$

$$3^x = y-2$$

$$3^{x+2} = y^{-1}$$

Example 4 $y = 6 \ln(3x) + 4$

$$x = 6 \ln(3y) + 4$$

$$x-4 = 6 \ln(3y)$$


$$\frac{x-4}{6} = \ln(3y)$$

$$e^{\frac{x-4}{6}} = 3y$$

$$\frac{e^{\frac{x-4}{6}}}{3} = y^{-1}$$

$$\frac{1}{3} \cdot e^{\frac{x-4}{6}} = y^{-1}$$

$$\begin{array}{l}
 x = \log_5 y^3 \\
 x = 3 \log_5 y \\
 \frac{x}{3} = \log_5 y \\
 y^{-1} = 5^{\frac{x}{3}}
 \end{array}
 \qquad
 \begin{array}{l}
 y = \log_5 x^3 \\
 x = \log_5 y^3 \\
 5^x = y^3 \\
 \sqrt[3]{5^x} = y
 \end{array}$$

$5^{\frac{x}{3}}$


$$\begin{array}{l}
 \sqrt[3]{5^x} \\
 \pm \sqrt[6]{5^x} = y^{-1}
 \end{array}$$