

Welcome to class!

-All cell phones in holder.

Time for a Quick Check-no
calculators.

$$\begin{aligned}\log_2 16 &= x \\ 2^x &= 16 \\ 2^x &= 2^4\end{aligned}$$

$$\begin{aligned}\log_2 16 + \log_5 125 \\ \log_2 2^4 + \log_5 5^3 \\ 4 + 3 = 7\end{aligned}$$

$$\begin{aligned}4\log_2 2 + 3\log_5 5 \\ 4 + 3 \\ 7\end{aligned}$$

Applications of LOGS

When applying logs to real-world situations, we will still use the same 4 formulas from last unit.

Growth: $A = P(1+r)^t$	Decay: $A = P(1-r)^t$
Compound Interest: $A = P\left(1 + \frac{r}{n}\right)^{n \cdot t}$	Compounded Continuously: $A = Pe^{rt}$

Now that we know how to solve logs we will be solving not only for A and P, but for rate (r) and time (t).

Example 1: \$500 is deposited in an account that pays 2% annual interest compounded continuously. Approximately how many years will it take for the account to reach \$1,000?

$$A = Pe^{rt}$$

$$1000 = 500e^{.02t}$$

$$2 = e^{.02t}$$

$$\ln 2 = .02t$$

$$34.7 = t$$

Example 2: A town of 1,000 people is experiencing an increase in population due to several new business openings. If the population increases at a rate of 5% per year, approximately how many years will it take for there to be 20,000 people in the town?

$$A = P(1+r)^t$$

$$20000 = 1000(1+.05)^t$$

$$20 = (1.05)^t$$

$$\log_{1.05}(20) = t$$

$$61.4 = t$$

$$61.4 \text{ years}$$

Example 3: You paid \$42,550 for a new car. If after 5 years the car is worth \$30,000, at what rate does the car decrease?

$$A = P(1-r)^t$$

$$30000 = 42,550(1-r)^5$$

$$\sqrt[5]{.71} = \sqrt[5]{(1-r)^5}$$

$$.933 = 1-r$$

$$\begin{array}{r} .933 \\ -1 \\ \hline -.067 = -r \end{array}$$

$$.067 = r \quad r = 6.7\%$$

Example 4: Brian would like to purchase a boat as a graduation present for himself. He deposits \$5,000 into an account that pays 7.5% interest compounded quarterly. If Brian needs \$50,000 in order to purchase the boat, how long will it take him to save enough money?

$$A = P\left(1 + \frac{r}{n}\right)^{nt}$$

$$50000 = 5000\left(1 + \frac{.075}{4}\right)^{4t}$$

$$10 = (1.01875)^{4t}$$

$$\log_{1.01875}(10) = 4t$$

$$30.99 = t$$

$$31 \text{ years}$$