

Welcome to class! Hope you are having a terrific Tuesday!

-All cell phones in holder

Take out homework sheet.

Solve

$$\begin{array}{r} x^2 + 144 = 0 \\ -144 \quad -144 \\ \hline \sqrt{x^2} = \sqrt{-144} \end{array}$$

$$x = \pm 12i$$

Describe the transformations by completing the table and then graph the given function using the parent graph and transformations as your guide. $f(x) = -(x-1)^2 + 4$

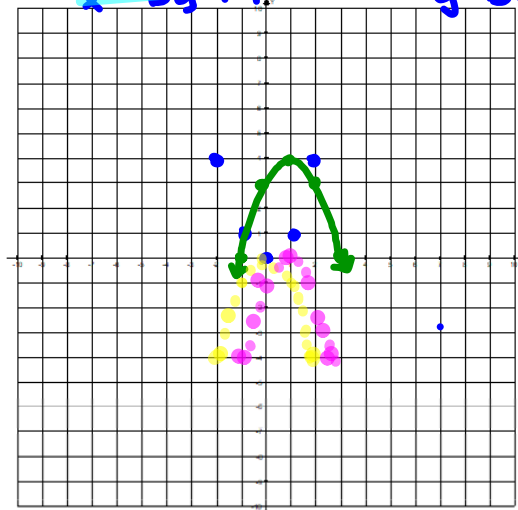
Parent Function	Reflection across x-axis?	Vertical Stretch? Shrink? What's the scale factor?	Horizontal Shift Right? Left? How many units?	Vertical shift Up? Down? How many units?
$y = x^2$	yes	None	Right 1	Up 4

Change y opposite

x by +1

y by +4

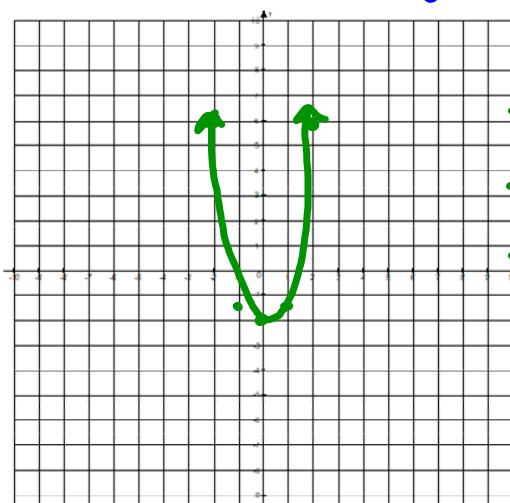
Key Points on parent function		Transformed Points to create the graph of your function	
x	y	x	y
-2	4	-1	0
-1	1	0	3
0	0	1	4
1	1	2	3
2	4	3	0



Describe the transformations by completing the table and then graph the given function using the parent graph and transformations as your guide. $f(x) = \frac{1}{2}x^4 - 2$

Parent Function	Reflection across x-axis?	Vertical Stretch? Shrink? What's the scale factor?	Horizontal Shift Right? Left? How many units?	Vertical shift Up? Down? How many units?
$y = x^4$	None	Compression by $\frac{1}{2}$ change y by $\frac{1}{2}$	None	down 2 $y - 2$

Key Points on parent function		Transformed Points to create the graph of your function	
x	y	x	y
-2	16	-2	6
-1	1	-1	-1.5
0	0	0	-2
1	1	1	-1.5
2	16	2	6

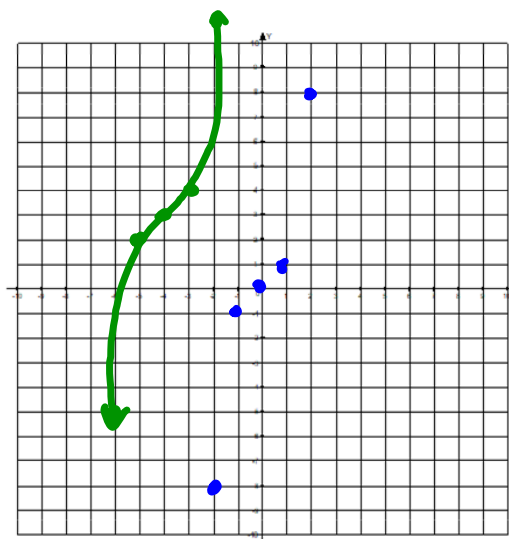


$$\begin{aligned} &\frac{1}{2}(16) - 2 \\ &\frac{1}{2}(1) - 2 \\ &\frac{1}{2}(0) - 2 \end{aligned}$$

Describe the transformations by completing the table and then graph the given function using the parent graph and transformations as your guide. $f(x) = (x + 4)^3 + 3$

Parent Function	Reflection across x-axis?	Vertical Stretch? Shrink? What's the scale factor?	Horizontal Shift Right? Left? How many units?	Vertical shift Up? Down? How many units?
$y =$				

Key Points on parent function		Transformed Points to create the graph of your function	
x	y	x	y
-2	-8	-6	-5
-1	-1	-5	+2
0	0	-4	3
1	1	-3	4
2	8	-2	11



Interval notation

$$y > 5 \quad \begin{array}{l} \text{Bigger} \\ \text{than 5} \\ \text{(not including 5)} \end{array} \quad (5, \infty)$$

$$y \geq 10 \quad \begin{array}{l} \text{Bigger than 10} \\ \text{(Include 10)} \end{array} \quad [10, \infty)$$

$$y < 3 \quad \begin{array}{l} \text{Smaller than 3} \\ \text{excluding 3} \end{array} \quad (-\infty, 3)$$

$$y \leq -2 \quad \begin{array}{l} \text{Smaller than -2} \\ \text{Include -2} \end{array} \quad (-\infty, -2]$$

Start, Stop [] =
Smallest, largest () not =

$$3 < y \leq 15 \quad (3, 15] \quad () \text{ not = the number}$$

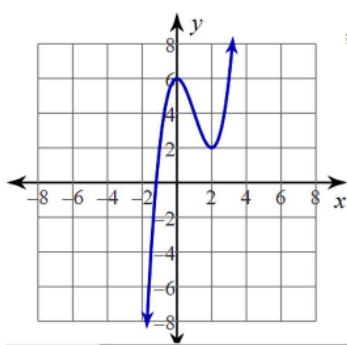
$$2 < y < 9 \quad (2, 9) \quad \cancel{[4, 7]}$$

Characteristics of Functions

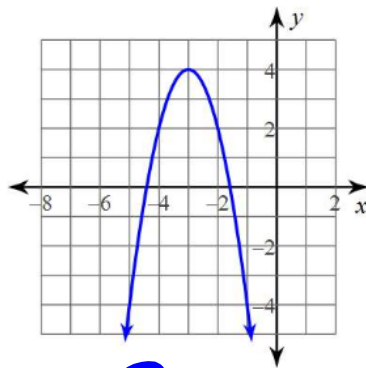
Domain: The set of all inputs. You look at the x-axis x-values to find the domain. You will always look left to Right.

\mathbb{R} or $(-\infty, \infty)$ means all real number.

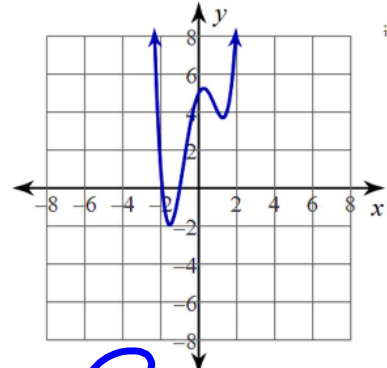
Examples:



\mathbb{R}



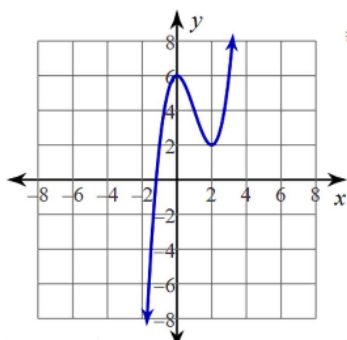
\mathbb{R}



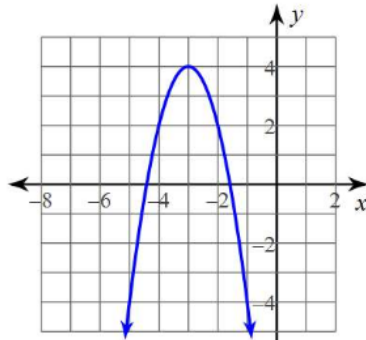
\mathbb{R}

Range: The set of all outputs. You look at the y-axis y-values to find the range. You will always look down to up.

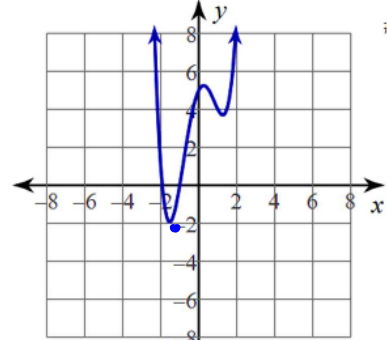
Examples:



$(-\infty, \infty)$



$(-\infty, 4]$



$[-2, \infty)$

x-intercepts: where the graph crosses the x-axis.

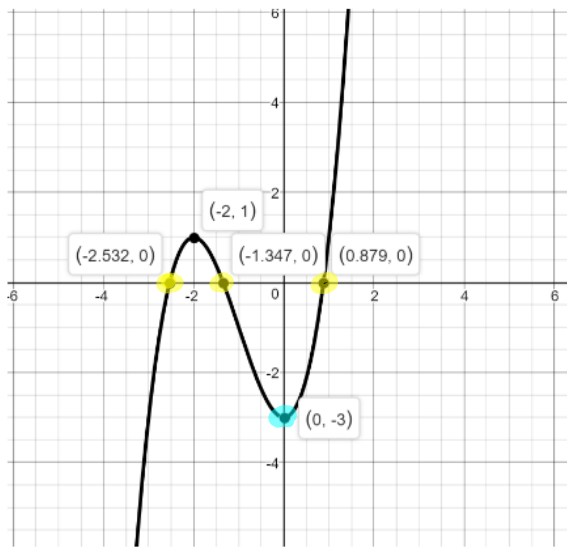
$$(x, 0)$$

y-intercepts: where the graph crosses the y-axis.

$$(0, y)$$

zeros: same as the x-intercepts but written differently.

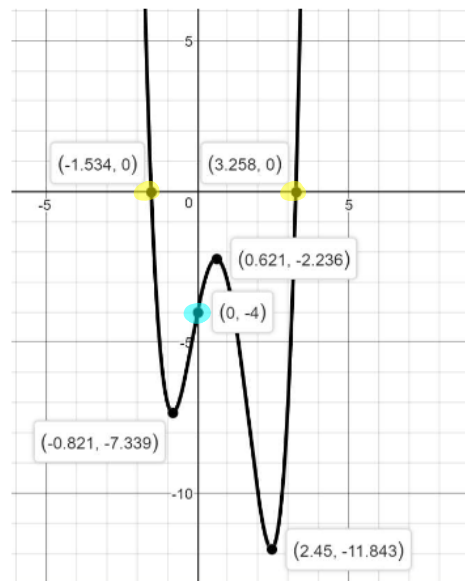
$$x = \#$$



Examples 1
 x-intercepts: $(-2.532, 0)$
 $(-1.347, 0)$
 $(0.879, 0)$

y-intercepts: $(0, -3)$

zeros: $x = -2.532$
 $x = -1.347$
 $x = 0.879$



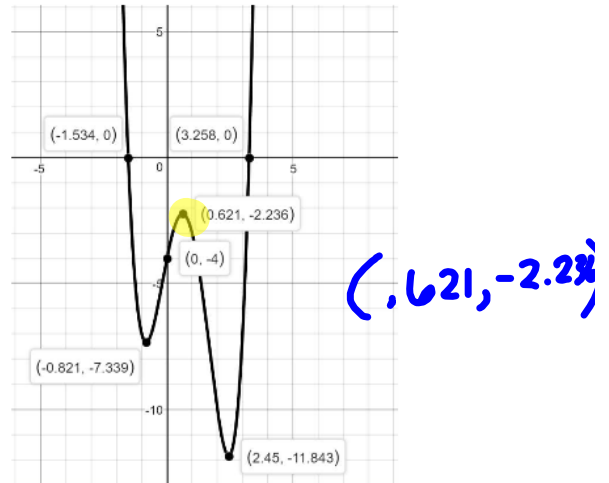
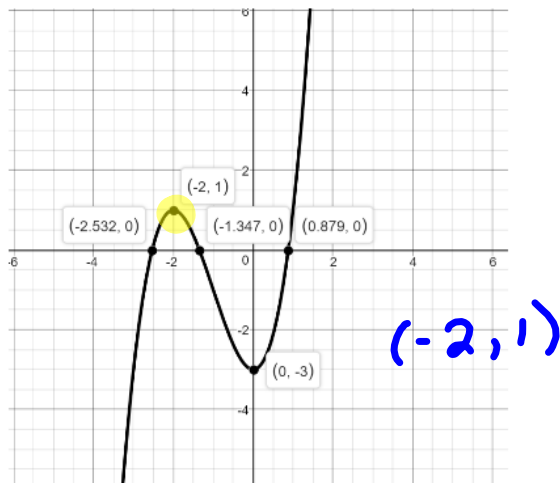
Examples 2
 x-intercepts: $(-1.534, 0)$
 $(3.258, 0)$

y-intercepts: $(0, -4)$

zeros: $x = -1.534$
 $x = 3.258$

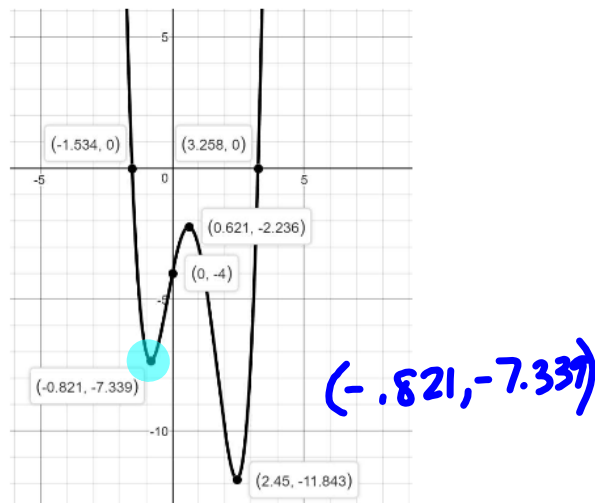
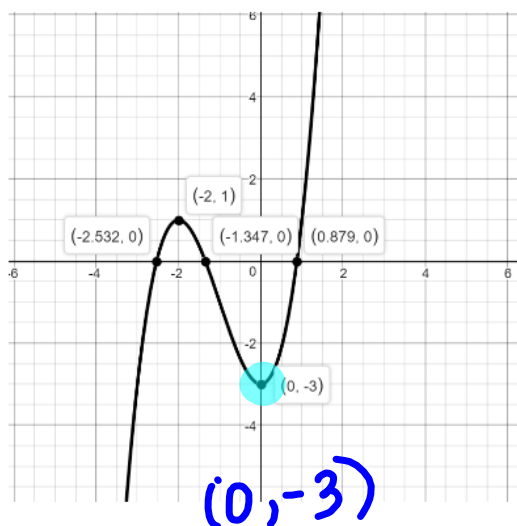
Relative Maximum: The highest point in a particular section of the graph (peak)

Examples:



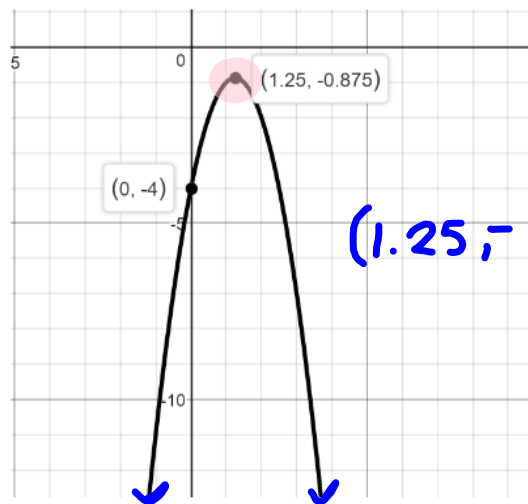
Relative Minimum: The lowest point in a particular section of the graph (dip)

Examples:

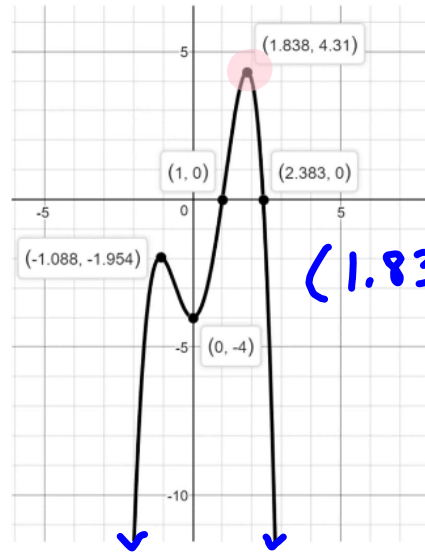


Absolute Maximum: The highest point over the **ENTIRE** domain of the graph.

Examples:



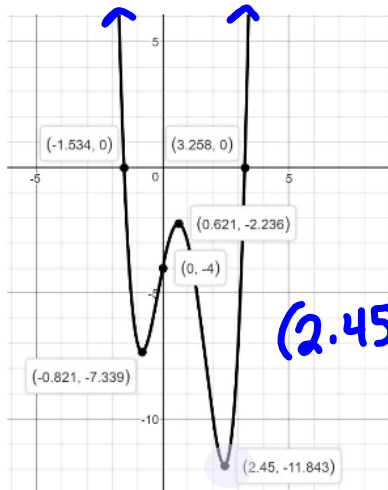
$(1.25, -0.875)$



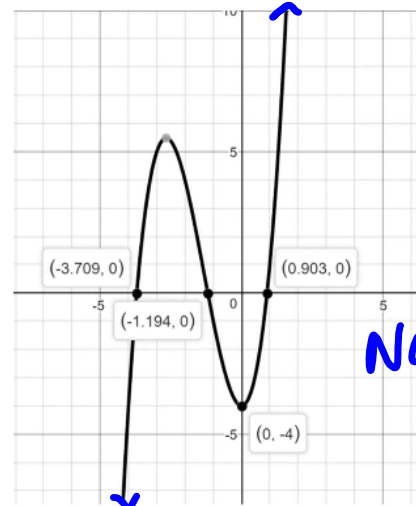
$(1.838, 4.31)$

Absolute Minimum: The lowest point over the **ENTIRE** domain of the graph.

Examples:



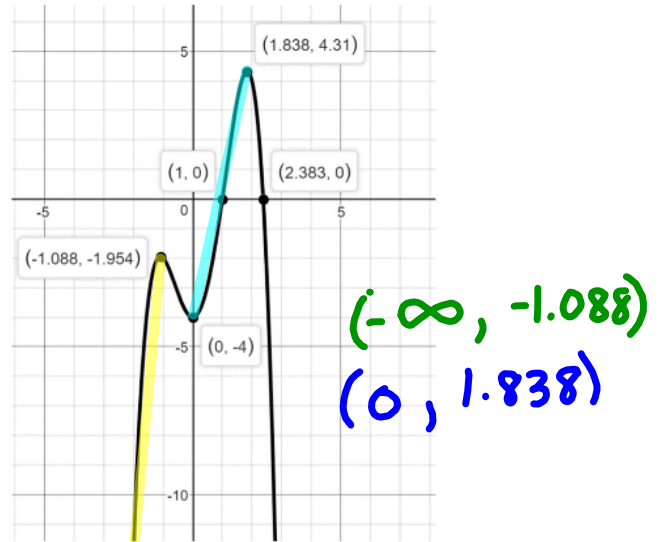
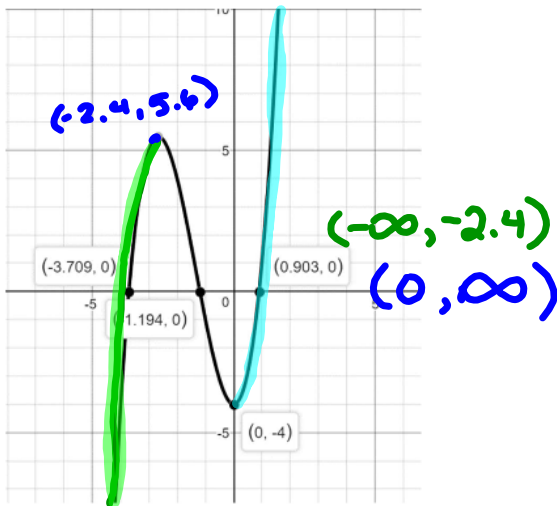
$(2.45, -11.843)$



NONE

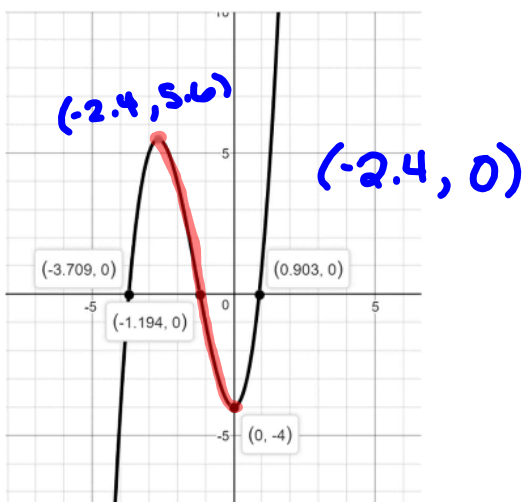
Interval of Increase: The set of values whereas x increases, $f(x)$ increases.

Examples: *x-values only*



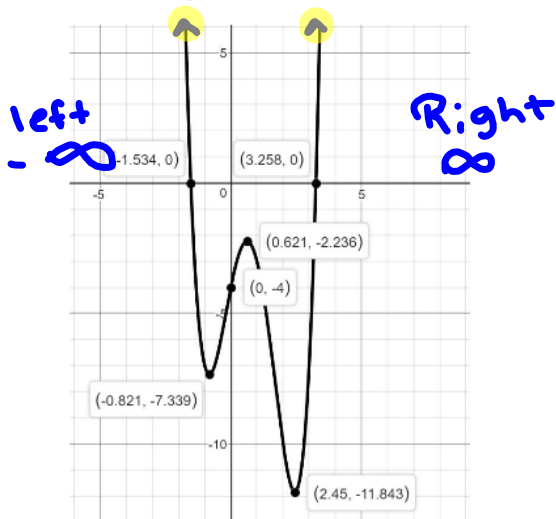
Interval of Decrease: The set of values whereas x increases, $f(x)$ decreases.

Examples:

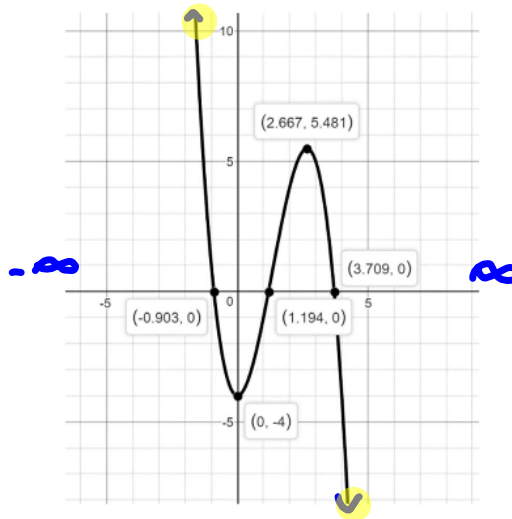


End Behavior: How does the graph act? Where do the arrows point?

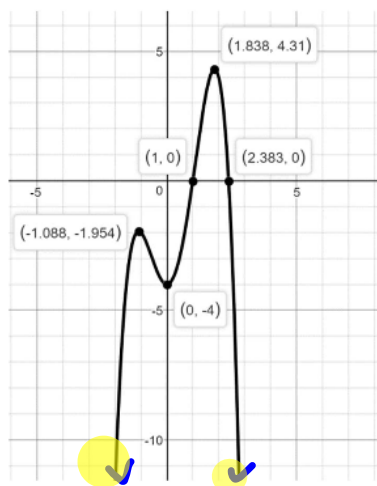
Examples:



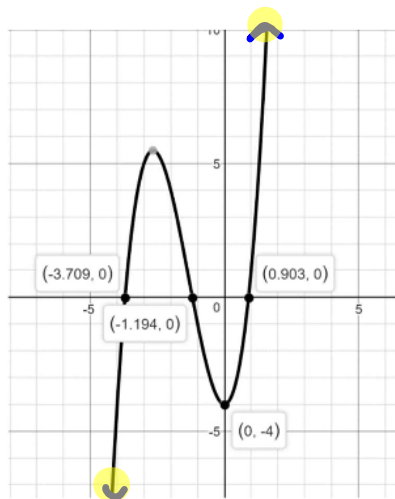
$x \rightarrow \underline{-\infty}, f(x) \rightarrow \underline{-\infty}$
 $x \rightarrow \underline{\infty}, f(x) \rightarrow \underline{\infty}$



$x \rightarrow \underline{\infty}, f(x) \rightarrow \underline{-\infty}$
 $x \rightarrow \underline{-\infty}, f(x) \rightarrow \underline{\infty}$



$x \rightarrow \underline{\infty}, f(x) \rightarrow \underline{-\infty}$
 $x \rightarrow \underline{-\infty}, f(x) \rightarrow \underline{-\infty}$



$x \rightarrow \underline{\infty}, f(x) \rightarrow \underline{\infty}$
 $x \rightarrow \underline{-\infty}, f(x) \rightarrow \underline{-\infty}$

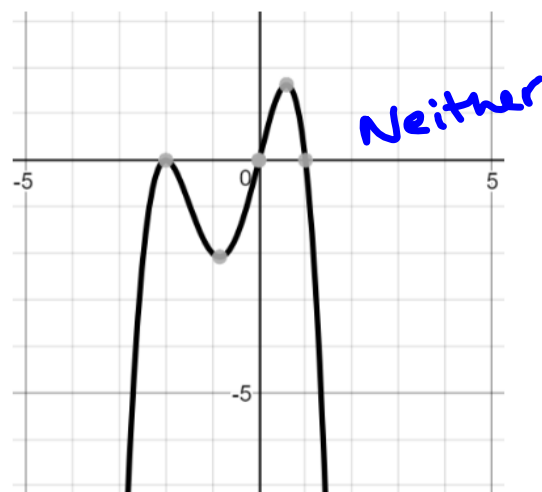
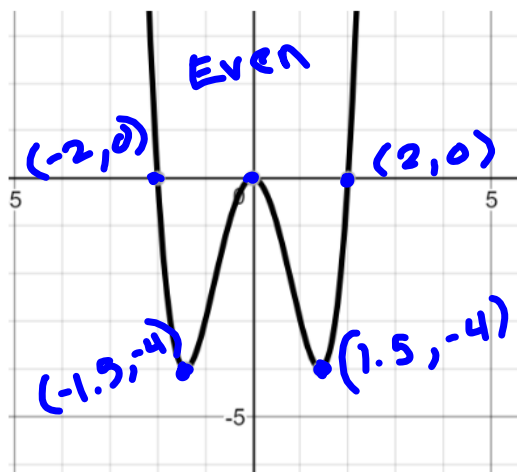
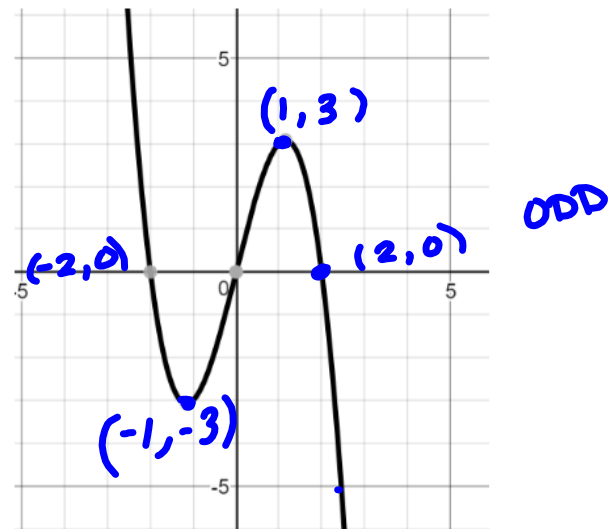
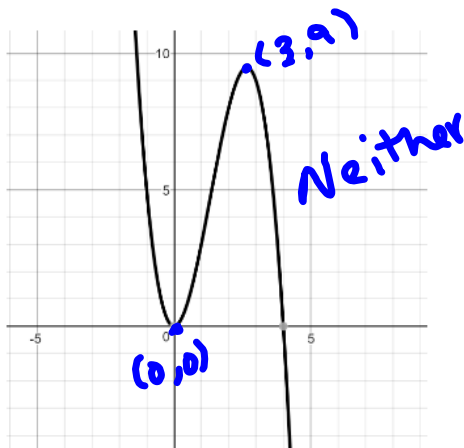
Symmetry:

Even - symmetric to the y-axis $(x, y) \rightarrow (-x, y)$

* Odd - symmetric to the origin $(x, y) \rightarrow (-x, -y)$

Neither – not symmetric to either y-axis or origin.

Examples:

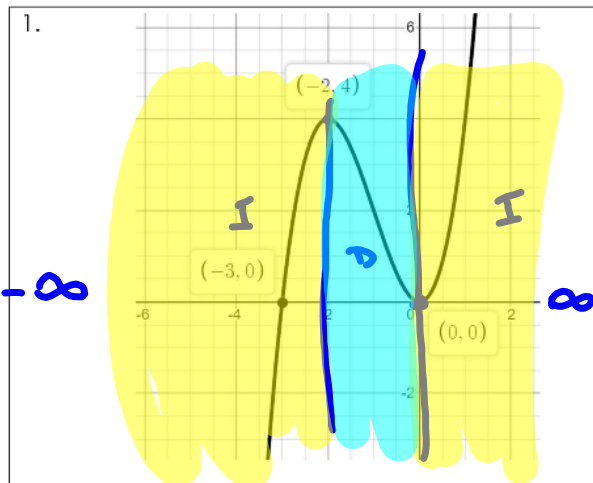


Characteristics of Polynomials

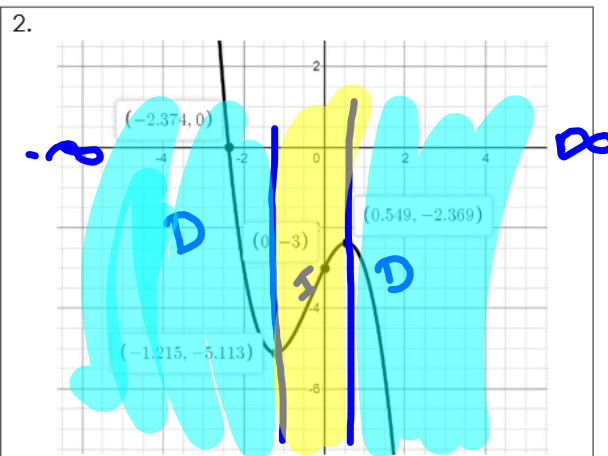
Name: _____

Practice

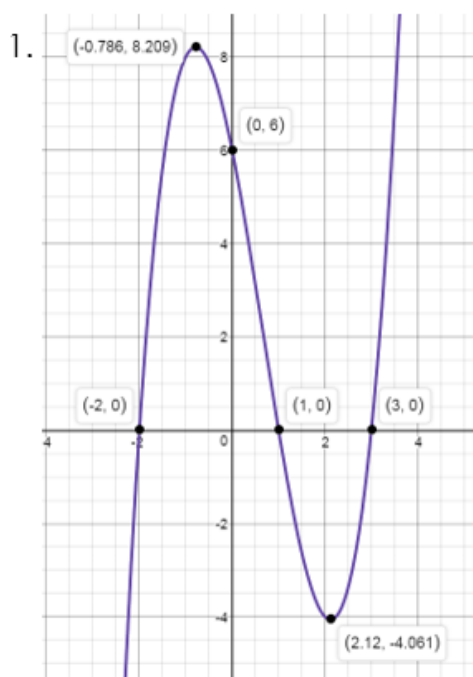
Date: _____ Block: _____



1.
 Domain \mathbb{R} Range $(-\infty, \infty)$
 Int. of Increase $(-\infty, -2)$ $(0, \infty)$
 Int. of decrease $(-2, 0)$
 Relative Maximum $(-2, 4)$
 Relative Minimum $(0, 0)$
 Absolute Maximum NONE
 Absolute Minimum NONE
 X intercept $(-3, 0)$ y-intercept $(0, 0)$
 Even/Odd/Neither Neither
 End Behavior $x \rightarrow \infty, f(x) \rightarrow \infty$
 $x \rightarrow -\infty, f(x) \rightarrow -\infty$

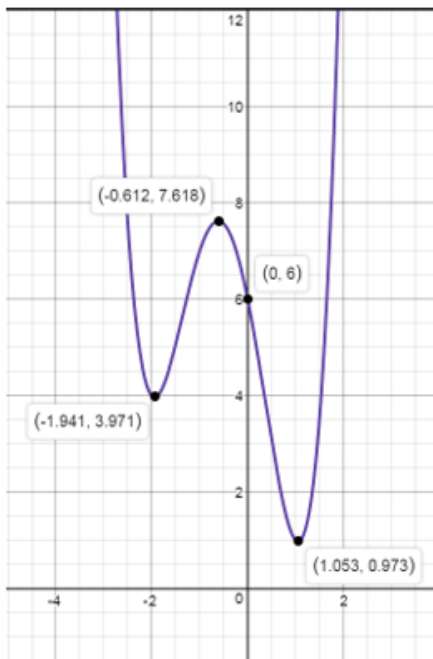


2.
 Domain \mathbb{R} Range $(-\infty, \infty)$
 Int. of Increase $(-1.215, .519)$
 Int. of decrease $(-\infty, -1.215)$ $(.519, \infty)$
 Relative Maximum $(.519, -2.369)$
 Relative Minimum $(-1.215, -5.113)$
 Absolute Maximum None
 Absolute Minimum None
 X intercept $(-2.374, 0)$ y-intercept $(0, -3)$
 Even/Odd/Neither Neither
 End Behavior $x \rightarrow \infty, f(x) \rightarrow -\infty$
 $x \rightarrow -\infty, f(x) \rightarrow \infty$



Domain \mathbb{R} Range $(-\infty, \infty)$
 Int. of Inc. $(-\infty, -0.786)$ Int. of dec. $(-0.786, 2.12)$
 Rel. Max $(-0.786, 8.209)$ Rel. Min $(2.12, -4.061)$
 Abs. Max N/A Abs. Min N/A
 X intercept $(-2, 0)$ $(1, 0)$ $(3, 0)$ y-intercept $(0, 6)$
 Zeros: $x = -2$ $x = 1$ $x = 3$ Even/Odd/Neither Neither
 End Behavior as $x \rightarrow \infty, f(x) \rightarrow \infty$
 as $x \rightarrow -\infty, f(x) \rightarrow -\infty$

2.



Domain \mathbb{R} Range $(.973, \infty)$
 $(-1.941, -.612)$ $(-\infty, -1.941)$
 Int. of Inc. $(1.053, \infty)$ Int. of dec. $(-.612, 1.053)$
 $(-.612, 7.618)$ $(-1.941, 3.971)$
 Rel. Max _____ Rel. Min _____
 Abs. Max None Abs. Min $(1.053, .973)$
 X intercept None y-intercept $(0, 6)$
 Zeros: None Even/Odd/Neither Neither
 End Behavior as $x \rightarrow \infty, f(x) \rightarrow \infty$
 as $x \rightarrow -\infty, f(x) \rightarrow \infty$

