

Welcome to Honors Algebra 2

-Cell phones in holder

Answers to Division

1) $x^2 + 3x + 8 - \frac{1}{3x + 3}$

2) $n^2 + 2n + 3 + \frac{3}{10n + 4}$

3) $10x^2 + 6x + 5 - \frac{9}{7x + 7}$

4) $v^2 - 2v + 9 + \frac{3}{2v + 10}$

5) $k^2 - 9k + 7 + \frac{5}{2k + 4}$

6) $4m^2 + 4m + 4 - \frac{8}{m + 3}$

7) $4k^2 + 9k + 7 - \frac{2}{k - 1}$

8) $n^2 - 6n - 2 + \frac{2}{n + 3}$

9) $b^2 + 3b + 9 - \frac{2}{b - 7}$

10) $n^2 + 4n - 5 - \frac{3}{n - 5}$

Operations with Functions

Adding Functions

$$(f+g)(x) = f(x) + g(x)$$

Subtracting Functions

$$(f-g)(x) = f(x) - g(x)$$

Multiplying Functions

$$(f \cdot g)(x) = [f(x)][g(x)]$$

(f ∘ g)(x)

Dividing Functions

$$(f/g)(x) = f(x)/g(x)$$

Let $f(x) = x - 5$ and $g(x) = x^2 - 2x - 15$.

Adding Functions

$$(f+g)(x) = f(x) + g(x)$$

Find $(f + g)(x)$.

$$(x-5) + (x^2 - 2x - 15)$$

$$\boxed{x^2 - x - 20}$$

Subtracting Functions

$$(f-g)(x) = f(x) - g(x)$$

Find $(g - f)(x)$

$$(x^2 - 2x - 15) - (x - 5)$$

$$\begin{array}{r} x^2 - 2x - 15 \\ - (x - 5) \\ \hline x^2 - 2x - 15 - x + 5 \end{array}$$

$$\boxed{x^2 - 3x - 10}$$

Let $f(x) = x - 5$ and $g(x) = x^2 - 2x - 15$.

Multiplying Functions

$$(f \cdot g)(x) = [f(x)][g(x)]$$

Find $(f \cdot g)(x)$.

$$(x - 5)(x^2 - 2x - 15)$$

$$\begin{array}{r} x^3 - 2x^2 - 15x \\ - 5x^2 + 10x + 75 \\ \hline x^3 - 7x^2 - 5x + 75 \end{array}$$

Let $f(x) = 6x^5 - 12x^3 - 15x$ and $g(x) = 3x$.

Dividing Functions

$$(f/g)(x) = f(x)/g(x)$$

Find $(f/g)(x)$.

$$\frac{6x^5 - 12x^3 - 15x}{3x} = 2x^4 - 4x^2 - 5$$

$$\frac{x-5}{x^2-2x-15}$$

Direct Substitution

- Plug x value into equation

Evaluate the following using each method

$$p(x) = x^2 - 5x + 3 \text{ for } p(-2)$$

$$x = -2$$

$$P(-2) = (-2)^2 - 5(-2) + 3$$

$$P(-2) = 17$$

$$x = -2 \quad y = 17$$

$$\star (-2, 17)$$

Synthetic Substitution

- use remainder of synthetic division

$$\begin{array}{r} \boxed{-2} \\ \hline 1 & -5 & 3 \\ & \downarrow & -2 & 14 \\ \hline 1 & -7 & \boxed{17} \end{array}$$

$$P(-2) = 17$$

$$\text{division } x^2 - 7 + \frac{17}{x+2}$$

Problems 1-3: Use synthetic substitution and direct substitution to evaluate the polynomial for the given value.

1. $P(x) = 2x^3 - 5x^2 + 7x - 3$ for $x = 4$

$$P(4) = 73$$

$$3. P(-2) = -8$$

2. $P(x) = 4x^3 - 7x^2 + 2x + 3$ for $x = -3$

$$P(-3) = -174$$

3. $P(x) = x^3 - x^2 + 4$ for $x = -2$

$$\begin{aligned} P(-2) &= (-2)^3 - (-2)^2 + 4 \\ &= -8 - 4 + 4 \\ &= -8 \end{aligned}$$

$$\begin{array}{r} -2 | 1 \ -1 \ 0 \ 4 \\ \downarrow \quad -2 \quad 6 \ -12 \\ 1 \ -3 \ 6 \ \boxed{-8} \end{array}$$

Add/Subtract Polynomial

Classify (degree term)

Mult. Polynomial

Binomial expansion (Pascal's) $\begin{array}{cccc} & & 1 & 1 \\ & & 1 & 2 \\ 1 & 3 & 3 & 1 \end{array}$

Division - Long

- Synthetic

Substitution - Direct

- Synthetic

Function/
function notation
 $(f+g)(x)$

