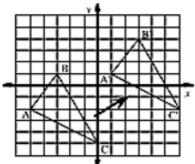
# Unit 2 Rigid Motion and Congruency

# Day 1 - Transformations

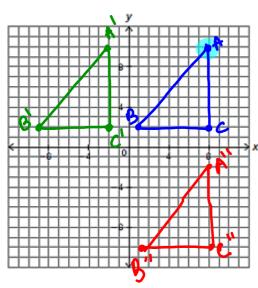
There are many different ways to move a figure on the coordinate plane. Some movements keep the figure the same size and some may make the figure bigger or smaller. These "movements" are called transformations. **Transformations** are the mapping or movement of all the points in a figure on the coordinate plane.



When a figure is the <u>original figure</u>, it is called the <u>pre-image</u>. The prefix "pre" means <u>before</u>. In the above picture, we would label the points as A, B, and C.

When a figure has been transformed, it is called the image. We would label the new points as A', B', and C'. We would say that points A, B, and C have been mapped to the new points A', B', and C'

# **Exploring Translations**



Observation: Did the figures change size or shape after each transformation?

- A. Graph triangle ABC by plotting points A(8, 10), B(1, 2), and C(8, 2).
- B. Translate triangle ABC 10 units to the left to form triangle A'B'C' and write new coordinates.
- C. Translate triangle ABC 12 units down to form triangle A"B"C" and write new coordinates.

Coordinates of Triangle ABC	Coordinates of Triangle A'B'C'	Coordinates of Triangle A"B"C"	
A (8, 10)	(-2,10)	(8,-2)	
B (1, 2)	(-9,2)	(1,-10)	
C(8, 2))	(-2,2)	(8,-10)	_
•	8-10=-2	10-12=	-'2
1	-10=-9	2-12=	10
É	-10=-2'	2-12=1	0

Geometry

Unit 2: Iransformations and Congruency

Notes

You observed that your four triangles maintained the same shape and size. When a figure keeps the same size and shape, it is called a **rigid transformation**.

With your experiment, you were performing a translation. A translation is a slide that maps all points of a figure the same distance in the same direction. A translation can slide a figure horizontally, vertically, or both.

# Rule for Translations: $(x, y) \rightarrow (x + a, y + b)$

- $\underline{\alpha} \rightarrow$  left or right translations (horizontally)
- b → up or down translations (vertically)

#### **Practice with Translations**

#### Practice:

g. ΔABC has vertices A(1, 2), B(3, 6), and C(9, 7).

What are the vertices after the triangle is

translated 4 units left?

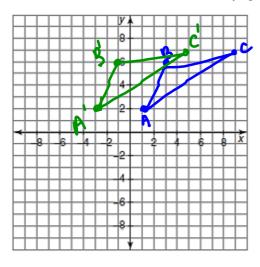
Rule:

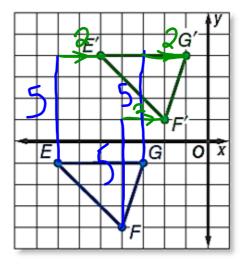
(x-4,y)

New Points: A'(-3,2) B'(-1,4) ('(5,7)

 $(\chi+2, y+5)$ 

b. Name the rule for the given figures;

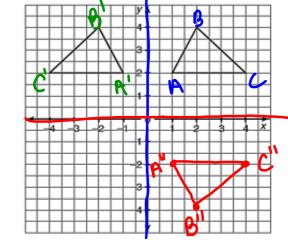




#### Reflections

1. Look at the two triangles in the figure. . Do you think they are congruent?

Figures that are mirror images of each other are called reflections. A reflection is a transformation that "flips" a figure over a reflection line. A reflection line is a line that acts as a mirror so that corresponding points are the same distance from the mirror. Reflections maintain shape and size; they are our second type of rigid transformation.



2. What do you think the reflection line is in the diagram?

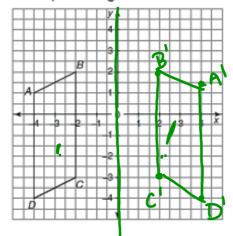
y-axis

- 3. Draw a triangle that would be a reflection over the x-axis.
- 4. What do you notice about the reflected triangles' points in relation to the pre-image?

Identical but opposite.

# Reflection over y-axis

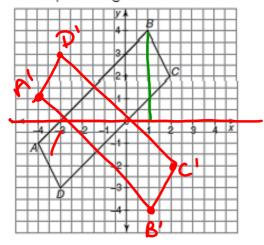
Reflect parallelogram ABCD over the y-axis using reflection lines. Record the points in the table.



	Pre-Image	Image
Α	(-4,1)	(4,1)
В	(-2.2)	(2, 2)
С	(-2:3)	(2,-3)
D	(-4,-4)	(4,-4)
Rule	(x, y)	(-x, y)

#### Reflection over x-axis

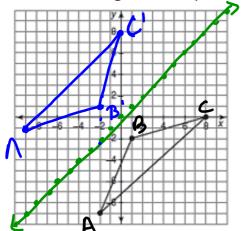
Reflect parallelogram ABCD over the x-axis using reflection lines. Record the points in the table



	Pre-Image	Image
Α	(-4,-1)	(-4,1)
В	(1,4)	(1,-4)
С	(2,2)	(2,-2)
D	(-3,-3)	(.3,3)
Rule	(x, y)	(x,-y)

# Reflection over y = x

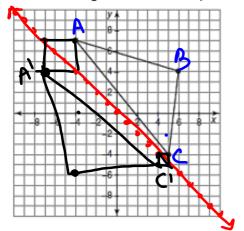
Reflect the triangle over the y = x using reflection lines. Record the points in the table



	Pre-Image	lmage
Α	(-1,-9)	(-9,-1)
В	(1,-2)	(-2,1)
С	(8,0)	(0,8)
Rule	(x, y)	(y,x)

# Reflection over y = -x

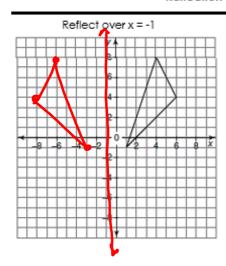
Reflect triangle ABC over the y = -x using reflection lines. Record the points in the table

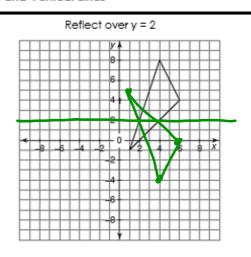


	Pre-Image	lmage
Α	(-4,7)	(-7,4)
В	(6,4)	(-4,-6)
С	(5,-4)	(4,-5)
Rule	(x, y)	(-4,-x)

4

#### Reflection over Horizontal and Vertical Lines



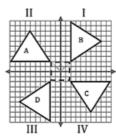


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Practice with Reflections			
Given triangle MNP with vertices of $M(1, 2)$ , $N(1, 4)$ , and $P(3, 3)$ , reflect across the following lines of reflection:			
x≂oxis (x. y)→	y-axis (x, y)->	y = x ( <u>x</u> . y)→	y = -x (x, y)→
M(1, 2) →	M(1, 2) →	M(1, 2) →	M(1, 2) →
N(1, 4) →	N(1, 4) →	N(1, 4) →	N(1, 4) →
P.(3, 3)→	P(3, 3)→	P(3, 3) →	P(3, 3)→

# Rotations, Symmetry, and Multiple Transformations

A rotation is a circular movement around a central point that stays fixed and everything else moves around that point in a circle. A rotation maintains size and shape; therefore, it is our third type of rigid transformation.



When we rotate our figures around a fixed point, we classify our rotation by direction and degree of rotation. Direction of Rotation

Degrees of Rotation









clockwise counterclockwise

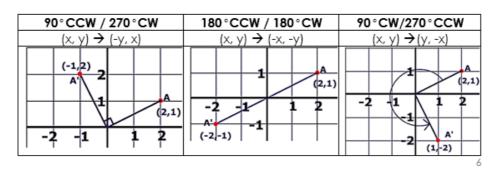
It is important to understand that some rotations are the same depending on the degree and direction of the rotation. Most of the time, rotations are given using counterclockwise direction. Here are equivalent rotations:

90 ° Counterclockwise = 270 ° Clockwise

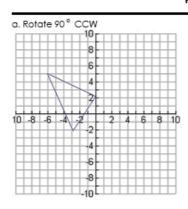
90 ° Clockwise = 270 ° Counterclockwise

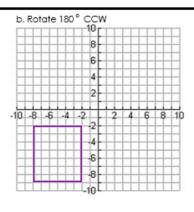
180 ° Counterclockwise = 180 ° Clockwise

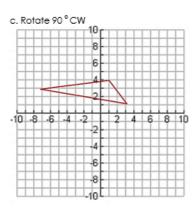
#### **Rules for Rotations**



#### **Practice with Rotations**







d. The line segment with endpoints (7, -8) and (-3, -5) are rotated 90 ° CW. What are its new endpoints?

#### **Rotational Symmetry**

A figure has **rotational symmetry** If there is a center point around which the object is turned a certain number of degrees and the object looks the same. The degree of rotational symmetry that an object has is called its **order**. The order of rotational symmetry that an object has is the number of times that it fits onto itself during a full rotation of 360 degrees. To determine the **angle of rotation**, divide 360 degrees by its order.

Example: Determine the order and angle of rotation:





**Practice:** For the following figures, name the order and degrees of rotation:



